

## Chapter 3

# Basic MapReduce Algorithm Design

A large part of the power of MapReduce comes from its simplicity: in addition to preparing the input data, the programmer needs only to implement the mapper, the reducer, and optionally, the combiner and the partitioner. All other aspects of execution are handled transparently by the execution framework—on clusters ranging from a single node to a few thousand nodes, over datasets ranging from gigabytes to petabytes. However, this also means that any conceivable algorithm that a programmer wishes to develop must be expressed in terms of a small number of rigidly-defined components that must fit together in very specific ways. It may not appear obvious how a multitude of algorithms can be recast into this programming model. The purpose of this chapter is to provide, primarily through examples, a guide to MapReduce algorithm design. These examples illustrate what can be thought of as “design patterns” for MapReduce, which instantiate arrangements of components and specific techniques designed to handle frequently-encountered situations across a variety of problem domains. Two of these design patterns are used in the scalable inverted indexing algorithm we’ll present later in Chapter 4; concepts presented here will show up again in Chapter 5 (graph processing) and Chapter 7 (expectation-maximization algorithms).

Synchronization is perhaps the most tricky aspect of designing MapReduce algorithms (or for that matter, parallel and distributed algorithms in general). Other than embarrassingly-parallel problems, processes running on separate nodes in a cluster must, at some point in time, come together—for example, to distribute partial results from nodes that produced them to the nodes that will consume them. Within a single MapReduce job, there is only one opportunity for cluster-wide synchronization—during the shuffle and sort stage where intermediate key-value pairs are copied from the mappers to the reducers and grouped by key. Beyond that, mappers and reducers run in isolation without any mechanisms for direct communication. Furthermore, the programmer has little control over many aspects of execution, for example:

- *Where* a mapper or reducer runs (i.e., on which node in the cluster).
- *When* a mapper or reducer begins or finishes.
- *Which* input key-value pairs are processed by a specific mapper.
- *Which* intermediate key-value pairs are processed by a specific reducer.

Nevertheless, the programmer does have a number of techniques for controlling execution and managing the flow of data in MapReduce. In summary, they are:

1. The ability to construct complex data structures as keys and values to store and communicate partial results.
2. The ability to execute user-specified initialization code at the beginning of a map or reduce task, and the ability to execute user-specified termination code at the end of a map or reduce task.
3. The ability to preserve state in both mappers and reducers across multiple input or intermediate keys.
4. The ability to control the sort order of intermediate keys, and therefore the order in which a reducer will encounter particular keys.
5. The ability to control the partitioning of the key space, and therefore the set of keys that will be encountered by a particular reducer.

It is important to realize that many algorithms cannot be easily expressed as a single MapReduce job. One must often decompose complex algorithms into a sequence of jobs, which requires orchestrating data so that the output of one job becomes the input to the next. Many algorithms are iterative in nature, requiring repeated execution until some convergence criteria—graph algorithms in Chapter 5 and expectation-maximization algorithms in Chapter 7 behave in exactly this way. Often, the convergence check itself cannot be easily expressed in MapReduce. The standard solution is an external (non-MapReduce) program that serves as a “driver” to coordinate MapReduce iterations.

This chapter explains how various techniques to control code execution and data flow can be applied to design algorithms in MapReduce. The focus is both on scalability—ensuring that there are no inherent bottlenecks as algorithms are applied to increasingly larger datasets—and efficiency—ensuring that algorithms do not needlessly consume resources and thereby reducing the cost of parallelization. The gold standard, of course, is linear scalability: an algorithm running on twice the amount of data should take only twice as long. Similarly, an algorithm running on twice the number of nodes should only take half as long.

The chapter is organized as follows:

- Section 3.1 introduces the important concept of local aggregation in MapReduce and strategies for designing efficient algorithms that minimize the amount of partial results that need to be copied across the network. The proper use of combiners is discussed in detail, as well as the “in-mapper combining” design pattern.
- Section 3.2 uses the example of building word co-occurrence matrices on large text corpora to illustrate two common design patterns, which we dub “pairs” and “stripes”. These two approaches are useful in a large class of problems that require keeping track of joint events across a large number of observations.
- Section 3.3 shows how co-occurrence counts can be converted into relative frequencies using a pattern known as “order inversion”. The sequencing of computations in the reducer can be recast as a sorting problem, where pieces of intermediate data are sorted into exactly the order that is required to carry out a series of computations. Often, a reducer needs to compute an aggregate statistic on a set of elements before individual elements can be processed. Normally, this would require two passes over the data, but with the “order inversion” design pattern, the aggregate statistic can be computed in the reducer before the individual elements are encountered. This may seem counter-intuitive: how can we compute an aggregate statistic on a set of elements before encountering elements of that set? As it turns out, clever sorting of special key-value pairs enables exactly this.
- Section 3.4 provides a general solution to secondary sorting, which is the problem of sorting values associated with a key in the reduce phase. We call this technique “value-to-key conversion”.

### 3.1 Local Aggregation

In the context of data-intensive distributed processing, the single most important aspect of synchronization is the exchange of intermediate results, from the processes that produced them to the processes that will ultimately consume them. In a cluster environment, with the exception of embarrassingly-parallel problems, this necessarily involves transferring data over the network. Furthermore, in Hadoop, intermediate results are written to local disk before being sent over the network. Since network and disk latencies are relatively expensive compared to other operations, reductions in the amount of intermediate data translate into increases in algorithmic efficiency. In MapReduce, local aggregation of intermediate results is one of the keys to efficient algorithms. Through use of the combiner and by taking advantage of the ability to preserve state across multiple inputs, it is often possible to substantially reduce both the number and size of key-value pairs that need to be shuffled from the mappers to the reducers.

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**Algorithm 3.1** Word count (repeated from Algorithm 2.1)

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The mapper emits an intermediate key-value pair for each word in a document. The reducer sums up all counts for each word.

```
1: class MAPPER
2:   method MAP(docid  $a$ , doc  $d$ )
3:     for all term  $t \in$  doc  $d$  do
4:       EMIT(term  $t$ , count 1)

1: class REDUCER
2:   method REDUCE(term  $t$ , counts [ $c_1, c_2, \dots$ ])
3:      $sum \leftarrow 0$ 
4:     for all count  $c \in$  counts [ $c_1, c_2, \dots$ ] do
5:        $sum \leftarrow sum + c$ 
6:     EMIT(term  $t$ , count  $sum$ )
```

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## Combiners and In-Mapper Combining

We illustrate various techniques for local aggregation using the simple word count example presented in Section 2.2. For convenience, Algorithm 3.1 repeats the pseudo-code of the basic algorithm, which is quite simple: the mapper emits an intermediate key-value pair for each term observed, with the term itself as the key and a value of one; reducers sum up the partial counts to arrive at the final count.

The first technique for local aggregation is the combiner, already discussed in Section 2.4. Combiners provide a general mechanism within the Map-Reduce framework to reduce the amount of intermediate data generated by the mappers—recall that they can be understood as “mini-reducers” that process the output of mappers. In this example, the combiners aggregate term counts across the documents processed by each map task. This results in a reduction in the number of intermediate key-value pairs that need to be shuffled across the network—from the order of *total* number of terms in the collection to the order of the number of *unique* terms in the collection.<sup>1</sup>

An improvement on the basic algorithm is shown in Algorithm 3.2 (the mapper is modified but the reducer remains the same as in Algorithm 3.1 and therefore is not repeated). An associative array (i.e., Map in Java) is introduced inside the mapper to tally up term counts within a single document: instead of emitting a key-value pair for each term in the document, this version emits a

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<sup>1</sup>More precisely, if the combiners take advantage of all opportunities for local aggregation, the algorithm would generate at most  $m \times V$  intermediate key-value pairs, where  $m$  is the number of mappers and  $V$  is the vocabulary size (number of unique terms in the collection), since every term could have been observed in every mapper. However, there are two additional factors to consider. Due to the Zipfian nature of term distributions, most terms will not be observed by most mappers (for example, terms that occur only once will by definition only be observed by one mapper). On the other hand, combiners in Hadoop are treated as *optional* optimizations, so there is no guarantee that the execution framework will take advantage of all opportunities for partial aggregation.

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**Algorithm 3.2** Word count mapper using associative arrays

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```
1: class MAPPER
2:   method MAP(docid  $a$ , doc  $d$ )
3:      $H \leftarrow$  new ASSOCIATIVEARRAY
4:     for all term  $t \in$  doc  $d$  do
5:        $H\{t\} \leftarrow H\{t\} + 1$             $\triangleright$  Tally counts for entire document
6:     for all term  $t \in H$  do
7:       EMIT(term  $t$ , count  $H\{t\}$ )
```

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---

**Algorithm 3.3** Word count mapper using the “in-mapper combining”

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```
1: class MAPPER
2:   method INITIALIZE
3:      $H \leftarrow$  new ASSOCIATIVEARRAY
4:   method MAP(docid  $a$ , doc  $d$ )
5:     for all term  $t \in$  doc  $d$  do
6:        $H\{t\} \leftarrow H\{t\} + 1$             $\triangleright$  Tally counts across documents
7:   method CLOSE
8:     for all term  $t \in H$  do
9:       EMIT(term  $t$ , count  $H\{t\}$ )
```

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key-value pair for each *unique* term in the document. Given that some words appear frequently within a document (for example, a document about dogs is likely to have many occurrences of the word “dog”), this can yield substantial savings in the number of intermediate key-value pairs emitted, especially for long documents.

This basic idea can be taken one step further, as illustrated in the variant of the word count algorithm in Algorithm 3.3 (once again, only the mapper is modified). The workings of this algorithm critically depends on the details of how map and reduce tasks in Hadoop are executed, discussed in Section 2.6. Recall, a (Java) mapper object is created for each map task, which is responsible for processing a block of input key-value pairs. Prior to processing any input key-value pairs, the mapper’s INITIALIZE method is called, which is an API hook for user-specified code. In this case, we initialize an associative array for holding term counts. Since it is possible to preserve state across multiple calls of the MAP method (for each input key-value pair), we can continue to accumulate partial term counts in the associative array *across* multiple documents, and emit key-value pairs only when the mapper has processed all documents. That is, emission of intermediate data is deferred until the CLOSE method in the pseudo-code. Recall that this API hook provides an opportunity to execute user-specified code *after* the MAP method has been applied to all input key-value pairs of the input data split to which the map task was assigned.

With this technique, we are in essence incorporating combiner functionality directly inside the mapper. There is no need to run a separate combiner,

since all opportunities for local aggregation are already exploited.<sup>2</sup> This is a sufficiently common design pattern in MapReduce that it's worth giving it a name, "in-mapper combining", so that we can refer to the pattern more conveniently throughout the book. We'll see later on how this pattern can be applied to a variety of problems. There are two main advantages to using this design pattern:

First, it provides control over when local aggregation occurs and how it exactly takes place. In contrast, the semantics of the combiner is underspecified in MapReduce. For example, Hadoop makes no guarantees on how many times the combiner is applied, or that it is even applied at all. The combiner is provided as a semantics-preserving optimization to the execution framework, which has the *option* of using it, perhaps multiple times, or not at all (or even in the reduce phase). In some cases (although not in this particular example), such indeterminism is unacceptable, which is exactly why programmers often choose to perform their own local aggregation in the mappers.

Second, in-mapper combining will typically be more efficient than using actual combiners. One reason for this is the additional overhead associated with actually materializing the key-value pairs. Combiners reduce the amount of intermediate data that is shuffled across the network, but don't actually reduce the number of key-value pairs that are emitted by the mappers in the first place. With the algorithm in Algorithm 3.2, intermediate key-value pairs are still generated on a per-document basis, only to be "compacted" by the combiners. This process involves unnecessary object creation and destruction (garbage collection takes time), and furthermore, object serialization and deserialization (when intermediate key-value pairs fill the in-memory buffer holding map outputs and need to be temporarily spilled to disk). In contrast, with in-mapper combining, the mappers will generate only those key-value pairs that need to be shuffled across the network to the reducers.

There are, however, drawbacks to the in-mapper combining pattern. First, it breaks the functional programming underpinnings of MapReduce, since state is being preserved across multiple input key-value pairs. Ultimately, this isn't a big deal, since pragmatic concerns for efficiency often trump theoretical "purity", but there are practical consequences as well. Preserving state across multiple input instances means that algorithmic behavior may depend on the order in which input key-value pairs are encountered. This creates the potential for ordering-dependent bugs, which are difficult to debug on large datasets in the general case (although the correctness of in-mapper combining for word count is easy to demonstrate). Second, there is a fundamental scalability bottleneck associated with the in-mapper combining pattern. It critically depends on having sufficient memory to store intermediate results until the mapper has completely processed all key-value pairs in an input split. In the word count example, the memory footprint is bound by the vocabulary size, since it is

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<sup>2</sup>Leaving aside the minor complication that in Hadoop, combiners can be run in the reduce phase also (when merging intermediate key-value pairs from different map tasks). However, in practice it makes almost no difference either way.

theoretically possible that a mapper encounters every term in the collection. Heap’s Law, a well-known result in information retrieval, accurately models the growth of vocabulary size as a function of the collection size—the somewhat surprising fact is that the vocabulary size never stops growing.<sup>3</sup> Therefore, the algorithm in Algorithm 3.3 will scale only up to a point, beyond which the associative array holding the partial term counts will no longer fit in memory.<sup>4</sup>

One common solution to limiting memory usage when using the in-mapper combining technique is to “block” input key-value pairs and “flush” in-memory data structures periodically. The idea is simple: instead of emitting intermediate data only after *every* key-value pair has been processed, emit partial results after processing every  $n$  key-value pairs. This is straightforwardly implemented with a counter variable that keeps track of the number of input key-value pairs that have been processed. As an alternative, the mapper could keep track of its own memory footprint and flush intermediate key-value pairs once memory usage has crossed a certain threshold. In both approaches, either the block size or the memory usage threshold needs to be determined empirically: with too large a value, the mapper may run out of memory, but with too small a value, opportunities for local aggregation may be lost. Furthermore, in Hadoop physical memory is split between multiple tasks that may be running on a node concurrently; these tasks are all competing for finite resources, but since the tasks are not aware of each other, it is difficult to coordinate resource consumption effectively. In practice, however, one often encounters diminishing returns in performance gains with increasing buffer sizes, such that it is not worth the effort to search for an *optimal* buffer size (personal communication, Jeff Dean).

In MapReduce algorithms, the extent to which efficiency can be increased through local aggregation depends on the size of the intermediate key space, the distribution of keys themselves, and the number of key-value pairs that are emitted by each individual map task. Opportunities for aggregation, after all, come from having multiple values associated with the same key (whether one uses combiners or employs the in-mapper combining pattern). In the word count example, local aggregation is effective because many words are encountered multiple times within a map task. Local aggregation is also an effective technique for dealing with reduce stragglers (see Section 2.3) that result from a highly-skewed (e.g., Zipfian) distribution of values associated with intermediate keys. In our word count example, we do not filter frequently-occurring words: therefore, without local aggregation, the reducer that’s responsible for computing the count of ‘the’ will have a lot more work to do than the typical reducer, and therefore will likely be a straggler. With local aggregation (either

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<sup>3</sup>In more detail, Heap’s Law relates the vocabulary size  $V$  to the collection size as follows:  $V = kT^b$ , where  $T$  is the number of tokens in the collection. Typical values of the parameters  $k$  and  $b$  are:  $30 \leq k \leq 100$  and  $b \sim 0.5$  ([101], p. 81).

<sup>4</sup>A few more details: note what matters is that the partial term counts encountered within particular *input split* fits into memory. However, as collection sizes increase, one will often want to increase the input split size to limit the growth of the number of map tasks (in order to reduce the number of distinct copy operations necessary to shuffle intermediate data over the network).

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**Algorithm 3.4** Compute the mean of values associated with the same key

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```
1: class MAPPER
2:   method MAP(string  $t$ , integer  $r$ )
3:     EMIT(string  $t$ , integer  $r$ )

1: class REDUCER
2:   method REDUCE(string  $t$ , integers [ $r_1, r_2, \dots$ ])
3:      $sum \leftarrow 0$ 
4:      $cnt \leftarrow 0$ 
5:     for all integer  $r \in$  integers [ $r_1, r_2, \dots$ ] do
6:        $sum \leftarrow sum + r$ 
7:        $cnt \leftarrow cnt + 1$ 
8:      $r_{avg} \leftarrow sum/cnt$ 
9:     EMIT(string  $t$ , integer  $r_{avg}$ )
```

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combiners or in-mapper combining), we substantially reduce the number of values associated with frequently-occurring terms, which alleviates the reduce straggler problem.

### Algorithmic Correctness with Local Aggregation

Although use of combiners can yield dramatic reductions in algorithm running time, care must be taken in applying them. Since combiners in Hadoop are viewed as optional optimizations, the correctness of the algorithm cannot depend on computations performed by the combiner or depend on them even being run at all. In any MapReduce program, the reducer input key-value type must match the mapper output key-value type: this implies that the combiner input *and* output key-value types must match the mapper output key-value type (which is the same as the reducer input key-value type). In cases where the reduce computation is both commutative and associative, the reducer can also be used (unmodified) as the combiner (as is the case with the word count example). In the general case, however, combiners and reducers are not interchangeable.

Consider a simple example: we have a large dataset where input keys are strings and input values are integers, and we wish to compute the mean of all integers associated with the same key (rounded to the nearest integer). A real-world example might be a large user log from a popular website, where keys represent user ids and values represent some measure of activity such as elapsed time for a particular session—the task would correspond to computing the mean session length on a per-user basis, which would be useful for understanding user demographics. Algorithm 3.4 shows the pseudo-code of a simple algorithm for accomplishing this task that does not involve combiners. We use an identity mapper, which simply passes all input key-value pairs to the reducers (appropriately grouped and sorted). The reducer keeps track of the running sum and the number of integers encountered. This information is used



to compute the mean once all values are processed. The mean is then emitted as the output value in the reducer (with the input string as the key).

This algorithm will indeed work, but suffers from the same drawbacks as the basic word count algorithm in Algorithm 3.1: it requires shuffling all key-value pairs from mappers to reducers across the network, which is highly inefficient. Unlike in the word count example, the reducer cannot be used as a combiner in this case. Consider what would happen if we did: the combiner would compute the mean of an arbitrary subset of values associated with the same key, and the reducer would compute the mean of those values. As a concrete example, we know that:

$$\text{MEAN}(1, 2, 3, 4, 5) \neq \text{MEAN}(\text{MEAN}(1, 2), \text{MEAN}(3, 4, 5)) \quad (3.1)$$

In general, the mean of means of arbitrary subsets of a set of numbers is not the same as the mean of the set of numbers. Therefore, this approach would not produce the correct result.<sup>5</sup>

So how might we properly take advantage of combiners? An attempt is shown in Algorithm 3.5. The mapper remains the same, but we have added a combiner that partially aggregates results by computing the numeric components necessary to arrive at the mean. The combiner receives each string and the associated list of integer values, from which it computes the sum of those values and the number of integers encountered (i.e., the count). The sum and count are packaged into a pair, and emitted as the output of the combiner, with the same string as the key. In the reducer, pairs of partial sums and counts can be aggregated to arrive at the mean. Up until now, all keys and values in our algorithms have been primitives (string, integers, etc.). However, there are no prohibitions in MapReduce for more complex types,<sup>6</sup> and, in fact, this represents a key technique in MapReduce algorithm design that we introduced at the beginning of this chapter. We will frequently encounter complex keys and values throughout the rest of this book.

Unfortunately, this algorithm will not work. Recall that combiners must have the same input and output key-value type, which also must be the same as the mapper output type and the reducer input type. This is clearly not the case. To understand why this restriction is necessary in the programming model, remember that combiners are optimizations that cannot change the correctness of the algorithm. So let us remove the combiner and see what happens: the output value type of the mapper is integer, so the reducer expects to receive a list of integers as values. But the reducer actually expects a list of pairs! The correctness of the algorithm is contingent on the combiner running on the output of the mappers, and more specifically, that the combiner is run exactly once. Recall from our previous discussion that Hadoop makes no

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<sup>5</sup>There is, however, one special case in which using reducers as combiners *would* produce the correct result: if each combiner computed the mean of equal-size subsets of the values. However, since such fine-grained control over the combiners is impossible in MapReduce, such a scenario is highly unlikely.

<sup>6</sup>In Hadoop, either custom types or types defined using a library such as Protocol Buffers, Thrift, or Avro.

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**Algorithm 3.5** Compute the mean of values associated with the same key

Note that this algorithm is incorrect. The mismatch between combiner input and output key-value types violates the MapReduce programming model.

```
1: class MAPPER
2:   method MAP(string t, integer r)
3:     EMIT(string t, integer r)

1: class COMBINER
2:   method COMBINE(string t, integers [r1, r2, ...])
3:     sum ← 0
4:     cnt ← 0
5:     for all integer r ∈ integers [r1, r2, ...] do
6:       sum ← sum + r
7:       cnt ← cnt + 1
8:     EMIT(string t, pair (sum, cnt))           ▷ Separate sum and count

1: class REDUCER
2:   method REDUCE(string t, pairs [(s1, c1), (s2, c2) ...])
3:     sum ← 0
4:     cnt ← 0
5:     for all pair (s, c) ∈ pairs [(s1, c1), (s2, c2) ...] do
6:       sum ← sum + s
7:       cnt ← cnt + c
8:     ravg ← sum/cnt
9:     EMIT(string t, integer ravg)
```

---

guarantees on how many times combiners are called; it could be zero, one, or multiple times. This violates the MapReduce programming model.

Another stab at the solution is shown in Algorithm 3.6, and this time, the algorithm is correct. In the mapper we emit as the value a pair consisting of the integer and one—this corresponds to a partial count over one instance. The combiner separately aggregates the partial sums and the partial counts (as before), and emits pairs with updated sums and counts. The reducer is similar to the combiner, except that the mean is computed at the end. In essence, this algorithm transforms a non-associative operation (mean of numbers) into an associative operation (element-wise sum of a pair of numbers, with an additional division at the very end).

Let us verify the correctness of this algorithm by repeating the previous exercise: What would happen if no combiners were run? With no combiners, the mappers would send pairs (as values) directly to the reducers. There would be as many intermediate pairs as there were input key-value pairs, and each of those would consist of an integer and one. The reducer would still arrive at the correct sum and count, and hence the mean would be correct. Now add in the combiners: the algorithm would remain correct, no matter how many times they run, since the combiners merely aggregate partial sums and counts

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**Algorithm 3.6** Compute the mean of values associated with the same key

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This algorithm correctly takes advantage of combiners.

```
1: class MAPPER
2:   method MAP(string t, integer r)
3:     EMIT(string t, pair (r, 1))

1: class COMBINER
2:   method COMBINE(string t, pairs [(s1, c1), (s2, c2) . . .])
3:     sum ← 0
4:     cnt ← 0
5:     for all pair (s, c) ∈ pairs [(s1, c1), (s2, c2) . . .] do
6:       sum ← sum + s
7:       cnt ← cnt + c
8:     EMIT(string t, pair (sum, cnt))

1: class REDUCER
2:   method REDUCE(string t, pairs [(s1, c1), (s2, c2) . . .])
3:     sum ← 0
4:     cnt ← 0
5:     for all pair (s, c) ∈ pairs [(s1, c1), (s2, c2) . . .] do
6:       sum ← sum + s
7:       cnt ← cnt + c
8:     ravg ← sum/cnt
9:     EMIT(string t, integer ravg)
```

---

to pass along to the reducers. Note that although the output key-value type of the combiner must be the same as the input key-value type of the reducer, the reducer can emit final key-value pairs of a different type.

Finally, in Algorithm 3.7, we present an even more efficient algorithm that exploits the in-mapper combining pattern. Inside the mapper, the partial sums and counts associated with each string are held in memory across input key-value pairs. Intermediate key-value pairs are emitted only after the entire input split has been processed; similar to before, the value is a pair consisting of the sum and count. The reducer is exactly the same as in Algorithm 3.6. Moving partial aggregation from the combiner directly into the mapper is subjected to all the tradeoffs and caveats discussed earlier this section, but in this case the memory footprint of the data structures for holding intermediate data is likely to be modest, making this variant algorithm an attractive option.

## 3.2 Pairs and Stripes

One common approach for synchronization in MapReduce is to construct complex keys and values in such a way that data necessary for a computation are naturally brought together by the execution framework. We first touched on this technique in the previous section, in the context of “packaging” partial

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**Algorithm 3.7** Compute the mean of values associated with the same key

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This mapper illustrates the in-mapper combining design pattern. The reducer is the same as in Algorithm 3.6

```
1: class MAPPER
2:   method INITIALIZE
3:      $S \leftarrow \text{new ASSOCIATIVEARRAY}$ 
4:      $C \leftarrow \text{new ASSOCIATIVEARRAY}$ 
5:   method MAP(string  $t$ , integer  $r$ )
6:      $S\{t\} \leftarrow S\{t\} + r$ 
7:      $C\{t\} \leftarrow C\{t\} + 1$ 
8:   method CLOSE
9:     for all term  $t \in S$  do
10:      EMIT(term  $t$ , pair ( $S\{t\}, C\{t\}$ ))
```

---

sums and counts in a complex value (i.e., pair) that is passed from mapper to combiner to reducer. Building on previously published work [54, 94], this section introduces two common design patterns we have dubbed “pairs” and “stripes” that exemplify this strategy.

As a running example, we focus on the problem of building word co-occurrence matrices from large corpora, a common task in corpus linguistics and statistical natural language processing. Formally, the co-occurrence matrix of a corpus is a square  $n \times n$  matrix where  $n$  is the number of unique words in the corpus (i.e., the vocabulary size). A cell  $m_{ij}$  contains the number of times word  $w_i$  co-occurs with word  $w_j$  within a specific context—a natural unit such as a sentence, paragraph, or a document, or a certain window of  $m$  words (where  $m$  is an application-dependent parameter). Note that the upper and lower triangles of the matrix are identical since co-occurrence is a symmetric relation, though in the general case relations between words need not be symmetric. For example, a co-occurrence matrix  $M$  where  $m_{ij}$  is the count of how many times word  $i$  was immediately succeeded by word  $j$  would usually not be symmetric.

This task is quite common in text processing and provides the starting point to many other algorithms, e.g., for computing statistics such as pointwise mutual information [38], for unsupervised sense clustering [136], and more generally, a large body of work in lexical semantics based on distributional profiles of words, dating back to Firth [55] and Harris [69] in the 1950s and 1960s. The task also has applications in information retrieval (e.g., automatic thesaurus construction [137] and stemming [157]), and other related fields such as text mining. More importantly, this problem represents a specific instance of the task of estimating distributions of discrete joint events from a large number of observations, a very common task in statistical natural language processing for which there are nice MapReduce solutions. Indeed, concepts presented here are also used in Chapter 7 when we discuss expectation-maximization algorithms.

Beyond text processing, problems in many application domains share sim-

ilar characteristics. For example, a large retailer might analyze point-of-sale transaction records to identify correlated product purchases (e.g., customers who buy *this* tend to also buy *that*), which would assist in inventory management and product placement on store shelves. Similarly, an intelligence analyst might wish to identify associations between re-occurring financial transactions that are otherwise unrelated, which might provide a clue in thwarting terrorist activity. The algorithms discussed in this section could be adapted to tackle these related problems.

It is obvious that the space requirement for the word co-occurrence problem is  $O(n^2)$ , where  $n$  is the size of the vocabulary, which for real-world English corpora can be hundreds of thousands of words, or even billions of words in web-scale collections.<sup>7</sup> The computation of the word co-occurrence matrix is quite simple if the entire matrix fits into memory—however, in the case where the matrix is too big to fit in memory, a naïve implementation on a single machine can be very slow as memory is paged to disk. Although compression techniques can increase the size of corpora for which word co-occurrence matrices can be constructed on a single machine, it is clear that there are inherent scalability limitations. We describe two MapReduce algorithms for this task that can scale to large corpora.

Pseudo-code for the first algorithm, dubbed the “pairs” approach, is shown in Algorithm 3.8. As usual, document ids and the corresponding contents make up the input key-value pairs. The mapper processes each input document and emits intermediate key-value pairs with each co-occurring word pair as the key and the integer one (i.e., the count) as the value. This is straightforwardly accomplished by two nested loops: the outer loop iterates over all words (the left element in the pair), and the inner loop iterates over all neighbors of the first word (the right element in the pair). The neighbors of a word can either be defined in terms of a sliding window or some other contextual unit such as a sentence. The MapReduce execution framework guarantees that all values associated with the same key are brought together in the reducer. Thus, in this case the reducer simply sums up all the values associated with the same co-occurring word pair to arrive at the absolute count of the joint event in the corpus, which is then emitted as the final key-value pair. Each pair corresponds to a cell in the word co-occurrence matrix. This algorithm illustrates the use of complex keys in order to coordinate distributed computations.

An alternative approach, dubbed the “stripes” approach, is presented in Algorithm 3.9. Like the pairs approach, co-occurring word pairs are generated by two nested loops. However, the major difference is that instead of emitting intermediate key-value pairs for each co-occurring word pair, co-occurrence information is first stored in an associative array, denoted  $H$ . The mapper emits key-value pairs with words as keys and corresponding associative arrays

---

<sup>7</sup>The size of the vocabulary depends on the definition of a “word” and techniques (if any) for corpus pre-processing. One common strategy is to replace all rare words (below a certain frequency) with a “special” token such as <UNK> (which stands for “unknown”) to model out-of-vocabulary words. Another technique involves replacing numeric digits with #, such that 1.32 and 1.19 both map to the same token (#.##).

---

**Algorithm 3.8** Compute word co-occurrence (“pairs” approach)

---

```
1: class MAPPER
2:   method MAP(docid  $a$ , doc  $d$ )
3:     for all term  $w \in \text{doc } d$  do
4:       for all term  $u \in \text{NEIGHBORS}(w)$  do
5:         EMIT(pair  $(w, u)$ , count 1)           ▷ Emit count for each
co-occurrence
1: class REDUCER
2:   method REDUCE(pair  $p$ , counts  $[c_1, c_2, \dots]$ )
3:      $s \leftarrow 0$ 
4:     for all count  $c \in \text{counts } [c_1, c_2, \dots]$  do
5:        $s \leftarrow s + c$                        ▷ Sum co-occurrence counts
6:     EMIT(pair  $p$ , count  $s$ )
```

---

---

**Algorithm 3.9** Compute word co-occurrence (“stripes” approach)

---

```
1: class MAPPER
2:   method MAP(docid  $a$ , doc  $d$ )
3:     for all term  $w \in \text{doc } d$  do
4:        $H \leftarrow \text{new ASSOCIATIVEARRAY}$ 
5:       for all term  $u \in \text{NEIGHBORS}(w)$  do
6:          $H\{u\} \leftarrow H\{u\} + 1$            ▷ Tally words co-occurring with  $w$ 
7:       EMIT(Term  $w$ , Stripe  $H$ )
1: class REDUCER
2:   method REDUCE(term  $w$ , stripes  $[H_1, H_2, H_3, \dots]$ )
3:      $H_f \leftarrow \text{new ASSOCIATIVEARRAY}$ 
4:     for all stripe  $H \in \text{stripes } [H_1, H_2, H_3, \dots]$  do
5:       SUM( $H_f, H$ )                             ▷ Element-wise sum
6:     EMIT(term  $w$ , stripe  $H_f$ )
```

---

as values, where each associative array encodes the co-occurrence counts of the neighbors of a particular word (i.e., its context). The MapReduce execution framework guarantees that all associative arrays with the same key will be brought together in the reduce phase of processing. The reducer performs an element-wise sum of all associative arrays with the same key, accumulating counts that correspond to the same cell in the co-occurrence matrix. The final associative array is emitted with the same word as the key. In contrast to the pairs approach, each final key-value pair encodes a row in the co-occurrence matrix.

It is immediately obvious that the pairs algorithm generates an immense number of key-value pairs compared to the stripes approach. The stripes representation is much more compact, since with pairs the left element is repeated for every co-occurring word pair. The stripes approach also generates fewer and shorter intermediate keys, and therefore the execution framework has less sorting to perform. However, values in the stripes approach are more complex, and come with more serialization and deserialization overhead than with the pairs approach.

Both algorithms can benefit from the use of combiners, since the respective operations in their reducers (addition and element-wise sum of associative arrays) are both commutative and associative. However, combiners with the stripes approach have more opportunities to perform local aggregation because the key space is the vocabulary—associative arrays can be merged whenever a word is encountered multiple times by a mapper. In contrast, the key space in the pairs approach is the cross of the vocabulary with itself, which is far larger—counts can be aggregated only when the same co-occurring word pair is observed multiple times by an individual mapper (which is less likely than observing multiple occurrences of a word, as in the stripes case).

For both algorithms, the in-mapper combining optimization discussed in the previous section can also be applied; the modification is sufficiently straightforward that we leave the implementation as an exercise for the reader. However, the above caveats remain: there will be far fewer opportunities for partial aggregation in the pairs approach due to the sparsity of the intermediate key space. The sparsity of the key space also limits the effectiveness of in-memory combining, since the mapper may run out of memory to store partial counts before all documents are processed, necessitating some mechanism to periodically emit key-value pairs (which further limits opportunities to perform partial aggregation). Similarly, for the stripes approach, memory management will also be more complex than in the simple word count example. For common terms, the associative array may grow to be quite large, necessitating some mechanism to periodically flush in-memory structures.

It is important to consider potential scalability bottlenecks of either algorithm. The stripes approach makes the assumption that, at any point in time, each associative array is small enough to fit into memory—otherwise, memory paging will significantly impact performance. The size of the associative array is bounded by the vocabulary size, which is itself unbounded with respect to corpus size (recall the previous discussion of Heap’s Law). There-

fore, as the sizes of corpora increase, this will become an increasingly pressing issue—perhaps not for gigabyte-sized corpora, but certainly for terabyte-sized and petabyte-sized corpora that will be commonplace tomorrow. The pairs approach, on the other hand, does not suffer from this limitation, since it does not need to hold intermediate data in memory.

Given this discussion, which approach is faster? Here, we present previously-published results [94] that empirically answered this question. We have implemented both algorithms in Hadoop and applied them to a corpus of 2.27 million documents from the Associated Press Worldstream (APW) totaling 5.7 GB.<sup>8</sup> Prior to working with Hadoop, the corpus was first preprocessed as follows: All XML markup was removed, followed by tokenization and stopword removal using standard tools from the Lucene search engine. All tokens were then replaced with unique integers for a more efficient encoding. Figure 3.1 compares the running time of the pairs and stripes approach on different fractions of the corpus, with a co-occurrence window size of two. These experiments were performed on a Hadoop cluster with 19 slave nodes, each with two single-core processors and two disks.

Results demonstrate that the stripes approach is much faster than the pairs approach: 666 seconds ( $\sim$ 11 minutes) compared to 3758 seconds ( $\sim$ 62 minutes) for the entire corpus (improvement by a factor of 5.7). The mappers in the pairs approach generated 2.6 billion intermediate key-value pairs totaling 31.2 GB. After the combiners, this was reduced to 1.1 billion key-value pairs, which quantifies the amount of intermediate data transferred across the network. In the end, the reducers emitted a total of 142 million final key-value pairs (the number of non-zero cells in the co-occurrence matrix). On the other hand, the mappers in the stripes approach generated 653 million intermediate key-value pairs totaling 48.1 GB. After the combiners, only 28.8 million key-value pairs remained. The reducers emitted a total of 1.69 million final key-value pairs (the number of rows in the co-occurrence matrix). As expected, the stripes approach provided more opportunities for combiners to aggregate intermediate results, thus greatly reducing network traffic in the shuffle and sort phase. Figure 3.1 also shows that both algorithms exhibit highly desirable scaling characteristics—linear in the amount of input data. This is confirmed by a linear regression applied to the running time data, which yields an  $R^2$  value close to one.

An additional series of experiments explored the scalability of the stripes approach along another dimension: the size of the cluster. These experiments were made possible by Amazon’s EC2 service, which allows users to rapidly provision clusters of varying sizes for limited durations (for more information, refer back to our discussion of utility computing in Section 1.1). Virtualized computational units in EC2 are called instances, and the user is charged only for the instance-hours consumed. Figure 3.2 (left) shows the running time of the stripes algorithm (on the same corpus, with same setup as before), on varying

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<sup>8</sup>This was a subset of the English Gigaword corpus (version 3) distributed by the Linguistic Data Consortium (LDC catalog number LDC2007T07).



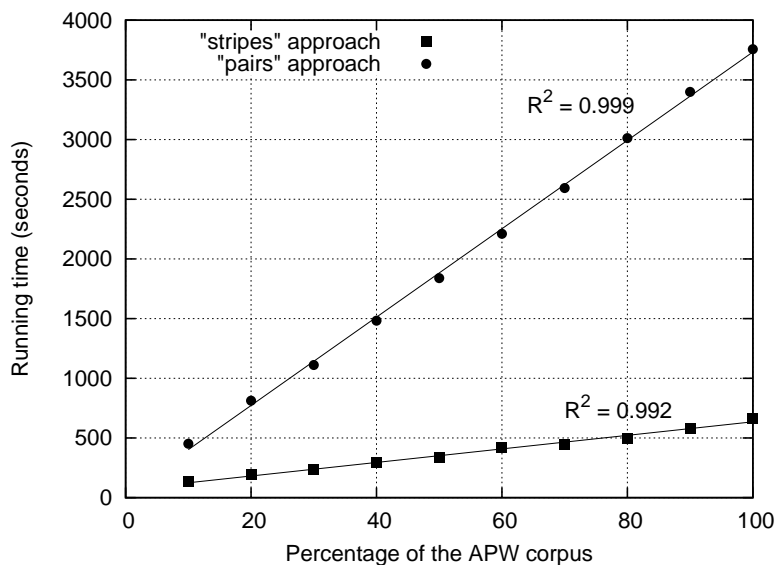


Figure 3.1: Running time of the “pairs” and “stripes” algorithms for computing word co-occurrence matrices on different fractions of the APW corpus. These experiments were performed on a Hadoop cluster with 19 slaves, each with two single-core processors and two disks.

cluster sizes, from 20 slave “small” instances all the way up to 80 slave “small” instances (along the  $x$ -axis). Running times are shown with solid squares. Figure 3.2 (right) recasts the same results to illustrate scaling characteristics. The circles plot the relative size and speedup of the EC2 experiments, with respect to the 20-instance cluster. These results show highly desirable linear scaling characteristics (i.e., doubling the cluster size makes the job twice as fast). This is confirmed by a linear regression with an  $R^2$  value close to one.

Viewed abstractly, the pairs and stripes algorithms represent two different approaches to counting co-occurring events from a large number of observations. This general description captures the gist of many algorithms in fields as diverse as text processing, data mining, and bioinformatics. For this reason, these two design patterns are broadly useful and frequently observed in a variety of applications.

To conclude, it is worth noting that the pairs and stripes approaches represent endpoints along a continuum of possibilities. The pairs approach individually records *each* co-occurring event, while the stripes approach records *all* co-occurring events with respect a conditioning event. A middle ground might be to record a subset of the co-occurring events with respect to a conditioning event. We might divide up the entire vocabulary into  $b$  buckets (e.g., via hashing), so that words co-occurring with  $w_i$  would be divided into  $b$  smaller

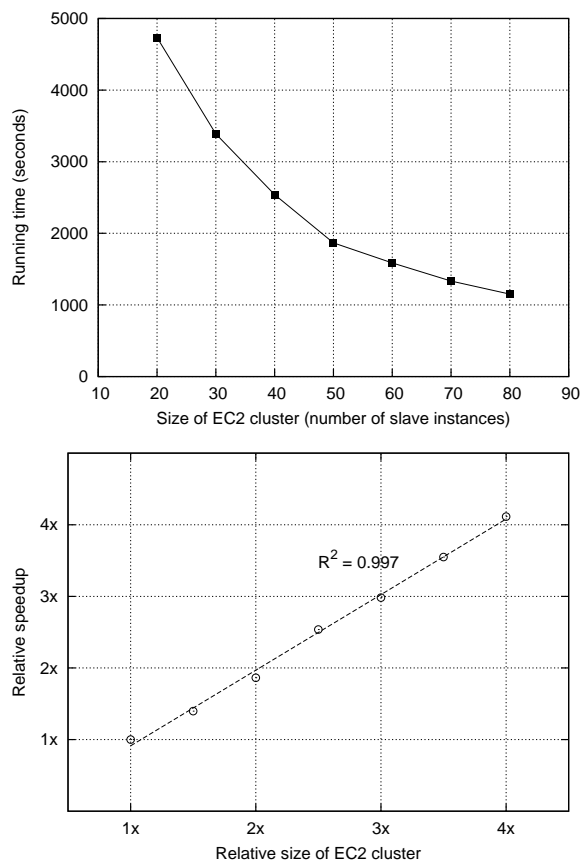


Figure 3.2: Running time of the stripes algorithm on the APW corpus with Hadoop clusters of different sizes from EC2 (left). Scaling characteristics (relative speedup) in terms of increasing Hadoop cluster size (right).

“sub-stripes”, associated with ten separate keys,  $(w_i, 1), (w_i, 2) \dots (w_i, b)$ . This would be a reasonable solution to the memory limitations of the stripes approach, since each of the sub-stripes would be smaller. In the case of  $b = |V|$ , where  $|V|$  is the vocabulary size, this is equivalent to the pairs approach. In the case of  $b = 1$ , this is equivalent to the standard stripes approach.

### 3.3 Computing Relative Frequencies

Let us build on the pairs and stripes algorithms presented in the previous section and continue with our running example of constructing the word co-occurrence matrix  $M$  for a large corpus. Recall that in this large square  $n \times n$

matrix, where  $n = |V|$  (the vocabulary size), cell  $m_{ij}$  contains the number of times word  $w_i$  co-occurs with word  $w_j$  within a specific context. The drawback of absolute counts is that it doesn't take into account the fact that some words appear more frequently than others. Word  $w_i$  may co-occur frequently with  $w_j$  simply because one of the words is very common. A simple remedy is to convert absolute counts into relative frequencies,  $f(w_j|w_i)$ . That is, what proportion of the time does  $w_j$  appear in the context of  $w_i$ ? This can be computed using the following equation:

$$f(w_j|w_i) = \frac{N(w_i, w_j)}{\sum_{w'} N(w_i, w')} \quad (3.2)$$

Here,  $N(\cdot, \cdot)$  indicates the number of times a particular co-occurring word pair is observed in the corpus. We need the count of the joint event (word co-occurrence), divided by what is known as the marginal (the sum of the counts of the conditioning variable co-occurring with anything else).

Computing relative frequencies with the stripes approach is straightforward. In the reducer, counts of all words that co-occur with the conditioning variable ( $w_i$  in the above example) are available in the associative array. Therefore, it suffices to sum all those counts to arrive at the marginal (i.e.,  $\sum_{w'} N(w_i, w')$ ), and then divide all the joint counts by the marginal to arrive at the relative frequency for all words. This implementation requires minimal modification to the original stripes algorithm in Algorithm 3.9, and illustrates the use of complex data structures to coordinate distributed computations in MapReduce. Through appropriate structuring of keys and values, one can use the Map-Reduce execution framework to bring together all the pieces of data required to perform a computation. Note that, as with before, this algorithm also assumes that each associative array fits into memory.

How might one compute relative frequencies with the pairs approach? In the pairs approach, the reducer receives  $(w_i, w_j)$  as the key and the count as the value. From this alone it is not possible to compute  $f(w_j|w_i)$  since we do not have the marginal. Fortunately, as in the mapper, the reducer can preserve state across multiple keys. Inside the reducer, we can buffer in memory all the words that co-occur with  $w_i$  and their counts, in essence building the associative array in the stripes approach. To make this work, we must define the sort order of the pair so that keys are first sorted by the left word, and then by the right word. Given this ordering, we can easily detect if all pairs associated with the word we are conditioning on ( $w_i$ ) have been encountered. At that point we can go back through the in-memory buffer, compute the relative frequencies, and then emit those results in the final key-value pairs.

There is one more modification necessary to make this algorithm work. We must ensure that all pairs with the same left word are sent to the same reducer. This, unfortunately, does not happen automatically: recall that the default partitioner is based on the hash value of the intermediate key, modulo the number of reducers. For a complex key, the raw byte representation is used to compute the hash value. As a result, there is no guarantee that, for

example, (dog, aardvark) and (dog, zebra) are assigned to the same reducer. To produce the desired behavior, we must define a custom partitioner that only pays attention to the left word. That is, the partitioner should partition based on the hash of the left word only.

This algorithm will indeed work, but it suffers from the same drawback as the stripes approach: as the size of the corpus grows, so does that vocabulary size, and at some point there will not be sufficient memory to store all co-occurring words and their counts for the word we are conditioning on. For computing the co-occurrence matrix, the advantage of the pairs approach is that it doesn't suffer from any memory bottlenecks. Is there a way to modify the basic pairs approach so that this advantage is retained?

As it turns out, such an algorithm is indeed possible, although it requires the coordination of several mechanisms in MapReduce. The insight lies in properly sequencing data presented to the reducer. If it were possible to somehow compute (or otherwise obtain access to) the marginal in the reducer before processing the joint counts, the reducer could simply divide the joint counts by the marginal to compute the relative frequencies. The notion of “before” and “after” can be captured in the ordering of key-value pairs, which can be explicitly controlled by the programmer. That is, the programmer can define the sort order of keys so that data needed earlier is presented to the reducer before data that is needed later. However, we still need to compute the marginal counts. Recall that in the basic pairs algorithm, each mapper emits a key-value pair with the co-occurring word pair as the key. To compute relative frequencies, we modify the mapper so that it additionally emits a “special” key of the form  $(w_i, *)$ , with a value of one, that represents the contribution of the word pair to the marginal. Through use of combiners, these partial marginal counts will be aggregated before being sent to the reducers. Alternatively, the in-mapper combining pattern can be used to even more efficiently aggregate marginal counts.

In the reducer, we must make sure that the special key-value pairs representing the partial marginal contributions are processed before the normal key-value pairs representing the joint counts. This is accomplished by defining the sort order of the keys so that pairs with the special symbol of the form  $(w_i, *)$  are ordered before any other key-value pairs where the left word is  $w_i$ . In addition, as with before we must also properly define the partitioner to pay attention to only the left word in each pair. With the data properly sequenced, the reducer can directly compute the relative frequencies.

A concrete example is shown in Figure 3.3, which lists the sequence of key-value pairs that a reducer might encounter. First, the reducer is presented with the special key (dog, \*) and a number of values, each of which represents a partial marginal contribution from the map phase (assume here either combiners or in-mapper combining, so the values represent partially aggregated counts). The reducer accumulates these counts to arrive at the marginal,  $\sum_{w'} N(\text{dog}, w')$ . The reducer holds on to this value as it processes subsequent keys. After (dog, \*), the reducer will encounter a series of keys representing joint counts; let's say the first of these is the key (dog, aardvark). Associated with this key

key	values	
(dog, *)	[6327, 8514, ...]	compute marginal: $\sum_{w'} N(\text{dog}, w') = 42908$
(dog, aardvark)	[2,1]	$f(\text{aardvark} \text{dog}) = 3/42908$
(dog, aardwolf)	[1]	$f(\text{aardwolf} \text{dog}) = 1/42908$
...		
(dog, zebra)	[2,1,1,1]	$f(\text{zebra} \text{dog}) = 5/42908$
(doge, *)	[682, ...]	compute marginal: $\sum_{w'} N(\text{doge}, w') = 1267$
...		

Figure 3.3: Example of the sequence of key-value pairs presented to the reducer in the pairs algorithm for computing relative frequencies. This illustrates the application of the order inversion design pattern.

will be a list of values representing partial joint counts from the map phase (two separate values in this case). Summing these counts will yield the final joint count, i.e., the number of times dog and aardvark co-occur in the entire collection. At this point, since the reducer already knows the marginal, simple arithmetic suffices to compute the relative frequency. All subsequent joint counts are processed in exactly the same manner. When the reducer encounters the next special key-value pair (doge, \*), the reducer resets its internal state and starts to accumulate the marginal all over again. Observe that the memory requirement for this algorithm is minimal, since only the marginal (an integer) needs to be stored. No buffering of individual co-occurring word counts is necessary, and therefore we have eliminated the scalability bottleneck of the previous algorithm.

This design pattern, which we call “order inversion”, occurs surprisingly often and across applications in many domains. It is so named because through proper coordination, we can access the result of a computation in the reducer (for example, an aggregate statistic) before processing the data needed for that computation. The key insight is to convert the sequencing of computations into a sorting problem. In most cases, an algorithm requires data in some fixed order: by controlling how keys are sorted and how the key space is partitioned, we can present data to the reducer in the order necessary to perform the proper computations. This greatly cuts down on the amount of partial results that the reducer needs to hold in memory.

To summarize, the specific application of the order inversion design pattern for computing relative frequencies requires the following:

- Emitting a special key-value pair for each co-occurring word pair in the mapper to capture its contribution to the marginal.
- Controlling the sort order of the intermediate key so that the key-value pairs representing the marginal contributions are processed by the reducer before any of the pairs representing the joint word co-occurrence counts.

- Defining a custom partitioner to ensure that all pairs with the same left word are shuffled to the same reducer.
- Preserving state across multiple keys in the reducer to first compute the marginal based on the special key-value pairs and then dividing the joint counts by the marginals to arrive at the relative frequencies.

As we will see in Chapter 4, this design pattern is also used in inverted index construction to properly set compression parameters for postings lists.

### 3.4 Secondary Sorting

MapReduce sorts intermediate key-value pairs by the keys during the shuffle and sort phase, which is very convenient if computations inside the reducer rely on sort order (e.g., the order inversion design pattern described in the previous section). However, what if in addition to sorting by key, we also need to sort by value? Google’s MapReduce implementation provides built-in functionality for (optional) secondary sorting, which guarantees that values arrive in sorted order. Hadoop, unfortunately, does not have this capability built in.

Consider the example of sensor data from a scientific experiment: there are  $m$  sensors each taking readings on continuous basis, where  $m$  is potentially a large number. A dump of the sensor data might look something like the following, where  $r_x$  after each timestamp represents the actual sensor readings (unimportant for this discussion, but may be a series of values, one or more complex records, or even raw bytes of images).

```
(t1, m1, r80521)
(t1, m2, r14209)
(t1, m3, r76042)
...
(t2, m1, r21823)
(t2, m2, r66508)
(t2, m3, r98347)
```

Suppose we wish to reconstruct the activity at each individual sensor over time. A MapReduce program to accomplish this might map over the raw data and emit the sensor id as the intermediate key, with the rest of each record as the value:

$$m_1 \rightarrow (t_1, r_{80521})$$

This would bring all readings from the same sensor together in the reducer. However, since MapReduce makes no guarantees about the ordering of values associated with the same key, the sensor readings will not likely be in temporal order. The most obvious solution is to buffer all the readings in memory and then sort by timestamp before additional processing. However, it should be apparent by now that any in-memory buffering of data introduces a potential

scalability bottleneck. What if we are working with a high frequency sensor or sensor readings over a long period of time? What if the sensor readings themselves are large complex objects? This approach may not scale in these cases—the reducer would run out of memory trying to buffer all values associated with the same key.

This is a common problem, since in many applications we wish to first group together data one way (e.g., by sensor id), and then sort within the groupings another way (e.g., by time). Fortunately, there is a general purpose solution, which we call the “value-to-key conversion” design pattern. The basic idea is to move part of the value into the intermediate key to form a composite key, and let the MapReduce execution framework handle the sorting. In the above example, instead of emitting the sensor id as the key, we would emit the sensor id and the timestamp as a composite key:

$$(m_1, t_1) \rightarrow (r_{80521})$$

The sensor reading itself now occupies the value. We must define the intermediate key sort order to first sort by the sensor id (the left element in the pair) and then by the timestamp (the right element in the pair). We must also implement a custom partitioner so that all pairs associated with the same sensor are shuffled to the same reducer.

Properly orchestrated, the key-value pairs will be presented to the reducer in the correct sorted order:

$$\begin{aligned} (m_1, t_1) &\rightarrow [(r_{80521})] \\ (m_1, t_2) &\rightarrow [(r_{21823})] \\ (m_1, t_3) &\rightarrow [(r_{146925})] \\ &\dots \end{aligned}$$

However, note that sensor readings are now split across multiple keys. The reducer will need to preserve state and keep track of when readings associated with the current sensor end and the next sensor begin.<sup>9</sup>

The basic tradeoff between the two approaches discussed above (buffer and in-memory sort vs. value-to-key conversion) is where sorting is performed. One can explicitly implement secondary sorting in the reducer, which is likely to be faster but suffers from a scalability bottleneck.<sup>10</sup> With value-to-key conversion, sorting is offloaded to the MapReduce execution framework. Note that this approach can be arbitrarily extended to tertiary, quaternary, etc. sorting. This pattern results in many more keys for the framework to sort, but distributed sorting is a task that the MapReduce runtime excels at since it lies at the heart of the programming model.

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<sup>9</sup>Alternatively, Hadoop provides API hooks to define “groups” of intermediate keys that should be processed together in the reducer.

<sup>10</sup>Note that, in principle, this need not be an in-memory sort. It is entirely possible to implement a disk-based sort within the reducer, although one would be duplicating functionality that is already present in the MapReduce execution framework. It makes more sense to take advantage of functionality that is already present with value-to-key conversion.

## 3.5 Summary

This chapter provides a guide on the design of MapReduce algorithms. In particular, we present a number of “design patterns” that capture effective solutions to common problems. In summary, they are:

- “In-mapper combining”, where the functionality of the combiner is moved into the mapper. Instead of emitting intermediate output for every input key-value pair, the mapper aggregates partial results across multiple input records and only emits intermediate key-value pairs after some amount of local aggregation is performed.
- The related patterns “pairs” and “stripes” for keeping track of joint events from a large number of observations. In the pairs approach, we keep track of each joint event separately, whereas in the stripes approach we keep track of all events that co-occur with the same event. Although the stripes approach is significantly more efficient, it requires memory on the order of the size of the event space, which presents a scalability bottleneck.
- “Order inversion”, where the main idea is to convert the sequencing of computations into a sorting problem. Through careful orchestration, we can send the reducer the result of a computation (e.g., an aggregate statistic) before it encounters the data necessary to produce that computation.
- “Value-to-key conversion”, which provides a scalable solution for secondary sorting. By moving part of the value into the key, we can exploit the MapReduce execution framework itself for sorting.

Ultimately, controlling synchronization in the MapReduce programming model boils down to effective use of the following techniques:

1. Constructing complex keys and values that bring together data necessary for a computation. This is used in all of the above design patterns.
2. Executing user-specified initialization and termination code in either the mapper or reducer. For example, in-mapper combining depends on emission of intermediate key-value pairs in the map task termination code.
3. Preserving state across multiple inputs in the mapper and reducer. This is used in in-mapper combining, order inversion, and value-to-key conversion.
4. Controlling the sort order of intermediate keys. This is used in order inversion and value-to-key conversion.
5. Controlling the partitioning of the intermediate key space. This is used in order inversion and value-to-key conversion.



This concludes our overview of MapReduce algorithm design. It should be clear by now that although the programming model forces one to express algorithms in terms of a small set of rigidly-defined components, there are many tools at one's disposal to shape the flow of computation. In the next few chapters, we will focus on specific classes of MapReduce algorithms: for inverted indexing in Chapter 4, for graph processing in Chapter 5, and for expectation-maximization in Chapter 7.