

# Opening the Black Box: Deriving Rules from Data

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# Opening the black box

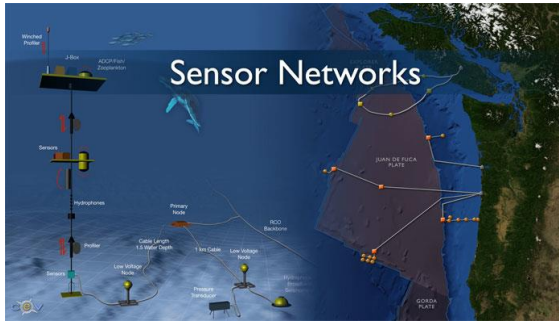
i.e., the long and winding road that takes to knowledge...





# Mining large datasets

- Continuously growing amounts of data are being collected and stored



Sensor data



User generated content



E-commerce data

- Available for exploration and analysis
  - Patterns and models are extracted from data to
    - describe their characteristics
    - predict variable values



# The Quest for Interpretability

- Powerful analysis techniques are being designed
  - Among them, deep learning techniques
- Unfortunately, many high quality models are characterized by being hardly interpretable
  - Data interpretability is important for decision making
- Rules mined from data may provide easily interpretable knowledge
  - both for exploration and classification (or prediction) purposes



# Extracting Meaning from Data

- Introducing some types of rules inferred from data
  - association rules
  - (associative) classification rules
  - with variations on the theme...
- Discussing their capability of
  - describing phenomena
  - giving meaning to the data under analysis



# Rule patterns

- High quality patterns derived bottom-up
  - Not assuming any apriori knowledge on data
    - will relax somewhat this hypothesis
- Several kinds of pattern
  - descriptive patterns: association rules & itemsets
  - rule models for prediction
- Focus on association rules
- Many application domains
  - Data exploration and explanation
  - Constraint derivation
  - ...



# Descriptive patterns

- Many different types of association-based patterns
  - itemsets
  - association rules
  - weighted association rules
  - generalized association rules



# Association rules

## ■ Objective

- extraction of frequent correlations or patterns from a transactional database

Purchases at a supermarket counter

| TID | Items                      |
|-----|----------------------------|
| 1   | Bread, Coke, Milk          |
| 2   | Beer, Bread                |
| 3   | Beer, Coke, Diapers, Milk  |
| 4   | Beer, Bread, Diapers, Milk |
| 5   | Coke, Diapers, Milk        |
| ... | ...                        |

## ■ Association rule

diapers  $\Rightarrow$  beer

- 2% of transactions contain both items
- 30% of transactions containing diapers also contain beer





# Transactional formats

- A transaction can be any set of items

- Market basket data

- Textual data

- A document is a transaction

- Words in a document are items in the transaction



- Structured data


- A table row is a transaction

- Pairs (attribute, value) are items in the transaction


- Example

Refund=no, MaritalStatus=married, TaxableIncome<80K, Cheat=No

| Tid | Refund | Marital Status | Taxable Income | Cheat |
|-----|--------|----------------|----------------|-------|
| 1   | Yes    | Single         | 125K           | No    |
| 2   | No     | Married        | 100K           | No    |
| 3   | No     | Single         | 70K            | No    |
| 4   | Yes    | Married        | 120K           | No    |
| 5   | No     | Divorced       | 95K            | Yes   |
| 6   | No     | Married        | 60K            | No    |
| 7   | Yes    | Divorced       | 220K           | No    |
| 8   | No     | Single         | 85K            | Yes   |
| 9   | No     | Married        | 75K            | No    |
| 10  | No     | Single         | 90K            | Yes   |



| Refund | Marital Status | Taxable Income | Cheat |
|--------|----------------|----------------|-------|
| No     | Married        | < 80K          | No    |



Example from: Tan, Steinbach, Kumar, Introduction to Data Mining, McGraw Hill 2006



# Association rules

- Identification of hidden correlations among data

$$X \rightarrow Y$$

- X and Y are itemsets, sets of one or more items
- Quality indices
  - *Support*: percentage of transactions containing X and Y
  - *Confidence*: conditional probability of finding Y given X
  - *Lift*: ratio between rule confidence and support of Y



# Considering weight

- Items may be characterized by different importance within a transaction
  - Examples: product quantity, term frequency of occurrence, tf-idf
- Weighted dataset
  - Each item is assigned a weight measuring its relevance in the corresponding transaction
- Weighted itemsets represent correlations among multiple highly relevant terms
  - Several different definitions of weighted itemset support



# Document summarization

- The summary of a collection of news documents ranging over the same topic
  - provides a synthetic overview of the most relevant news facets
  - does not require access to the entire document collection
- Itemset-based summarizers analyze the co-occurrences between multiple document terms
  - frequent weighted itemsets consider only the correlations between *highly relevant* terms
  - term weights measure term relevance in the analyzed collection



# Document summarization

- Language-agnostic approach
  - makes minimal use of language-dependent analyses (stopwords, optionally stemming)
  - is easily applicable to document collections written in different languages (Arabic, Czech, English, French, Greek, Hindi)
- Item weights are particularly effective for summarizing documents written in languages other than English

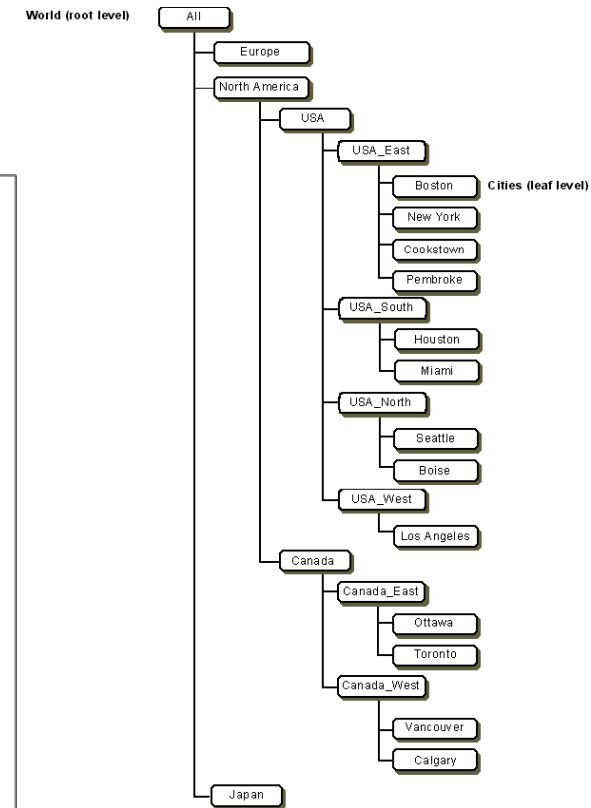
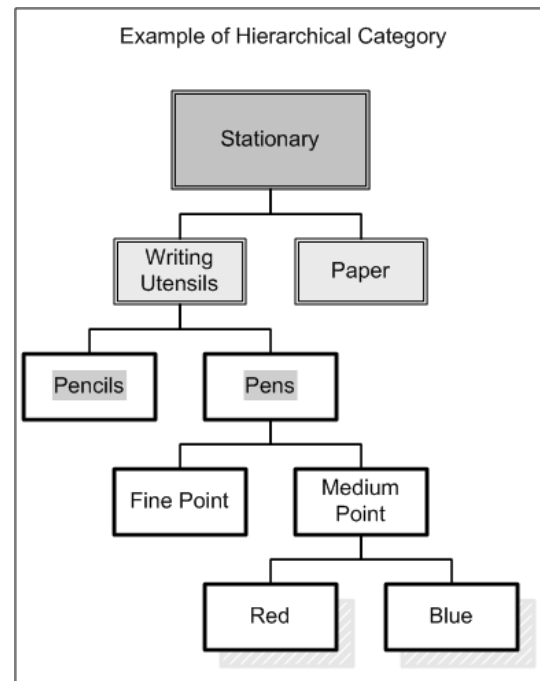
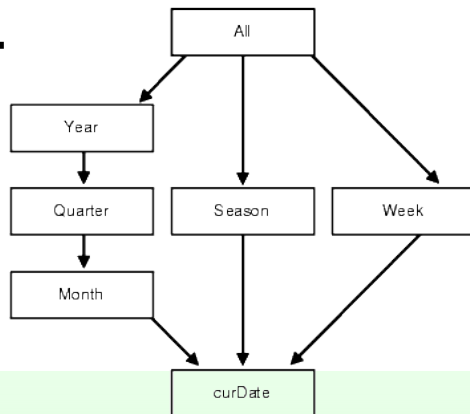


# Considering hierarchies

- Generalization hierarchies
  - Aggregation over attributes in a dataset
  - Typically user provided

- Examples

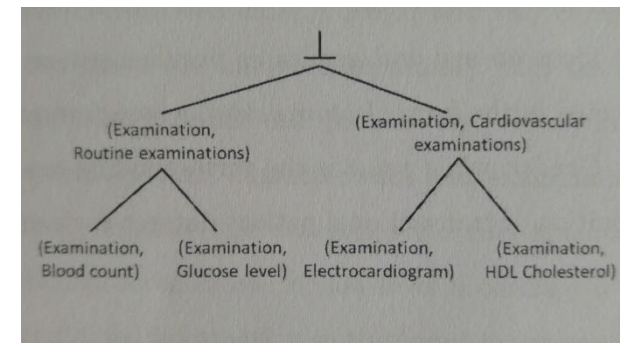
- Time hierarchy
- Product category
- Location hierarchy
- ...





# Taxonomy

- A taxonomy is a set of is-a hierarchies that aggregate data items into higher-level concepts
- Data item
  - Instance in the (transactional) dataset
  - Represents detailed concepts
- Generalized item
  - Aggregation in higher-level concepts
  - Represents abstractions on instances





# Generalized itemsets

- Sets of items at different generalization levels
  - May contain data items together with generalized items defined in the taxonomy
  - Summarize knowledge represented by a set of lower-level descendants
    - Both frequent and infrequent
- A generalized itemset covers a transaction when all
  - its generalized items are ancestors of items included in the transaction
  - its data items are included in the transaction
- Generalized itemset support
  - ratio between number of covered transactions and dataset cardinality





# Context-aware data analysis

- Context data provided by different, possibly heterogeneous, sources
  - Mobile devices provide information on
    - the user context (e.g., GPS coordinates)
    - the supplied services
      - temporal information
      - service description
      - duration
  - Additional information available
    - demographics of the user requesting the service



# Generalized itemset example

***user: John, time: 6.05 p.m., service: Weather***  
**(s = 0.005%)**

- A very low support
  - The itemset may be discarded
- By generalizing
  - the time attribute on a time period
  - the user on a user category

***user: employee, time: 6 p.m. to 7 p.m., service: Weather***  
**(s = 0.2%)**

- May discover interesting properties generalizing *infrequent* items



# Generalized association rules

- Extension of “classical” association rules

$$X \rightarrow Y$$

- X and Y are either generalized or not generalized itemsets
  - Support, confidence and lift are defined accordingly



# Patient data analysis

- Analysis of multiple level correlations on patient treatment historical data
  - Dataset collected by an Italian Local Health Center
    - Diabetes complications at various severity levels
    - 95K records, 3.5K patients
  - Features
    - Prescribed examinations (26 examinations, 7 categories)
    - Prescribed drugs (200 drugs, 14 categories)
    - Census patient data (gender, age discretized in age groups)
- Sparse dataset
  - Difficult setting of support threshold
    - Low: generates too many rules
    - High: interesting information at lower levels of abstraction may remain hidden



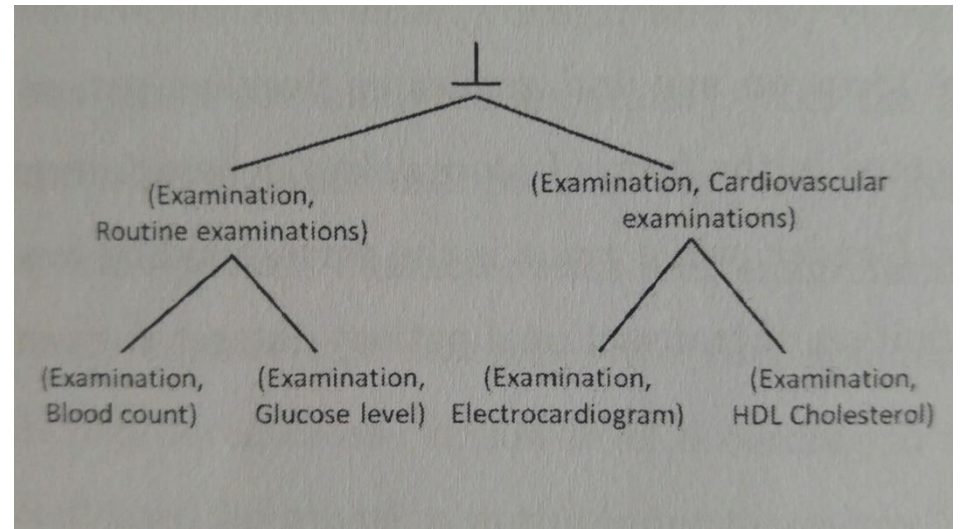
# Patient data analysis

- Rule exploration in top-down fashion
  - From small subset of high-level rules drill down to more specific rules
    - Descending level of abstraction on the considered taxonomy
  - Discovery of rule groups at different abstraction levels
    - Typically more manageable for manual exploration
- Consider only non redundant rules
  - Compact subset based on closed itemsets
    - Rule is redundant if it has same support and confidence of its specialized version
  - Reduces cardinality of rule set



# Patient data analysis

- High-level rules
  - Only generalized itemsets (examination and drug categories)
  - Represent general knowledge
    - May be too high level to perform targeted analyses



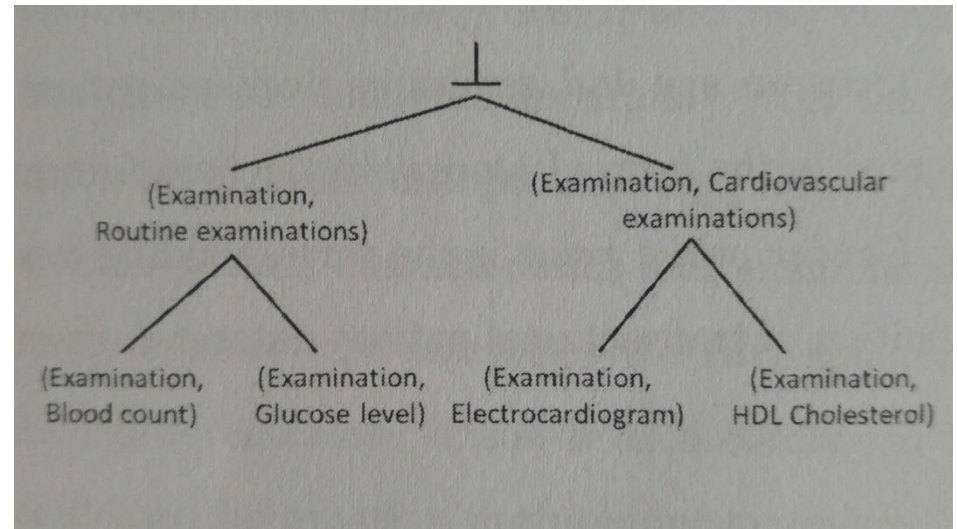


# Patient data analysis

- Extracted high-level rule

(Examination, Liver) -> (Examination, Kidney)

- Frequently prescribed together
- May be used for examination scheduling





# Patient data analysis

- Cross-level rules

- Different abstraction levels (generalized items and data items)
- Combine detailed and general information

- Extracted cross-level rule

(Examination, Liver) -> (Examination, Uric acid)

- Insight into specific kidney examinations correlated with liver examinations
  - Confidence: 74.8%





# Patient data analysis

- Low-level rules
  - Only not generalized itemsets (only data items)
  - Very detailed knowledge
    - Covered by high and cross-level rules
  - Large rule set
    - Challenging exploration task
  - Drill down exploration based on formerly extracted high and cross-level rules



# Outcomes

- Allow experts to
  - Identify medical treatments commonly followed by patients with a given disease
  - Verify adherence of medical treatment to shared medical guidelines
  - Improve the effectiveness of medical treatments
  - Plan resource allocation and reduce costs incurred by organization



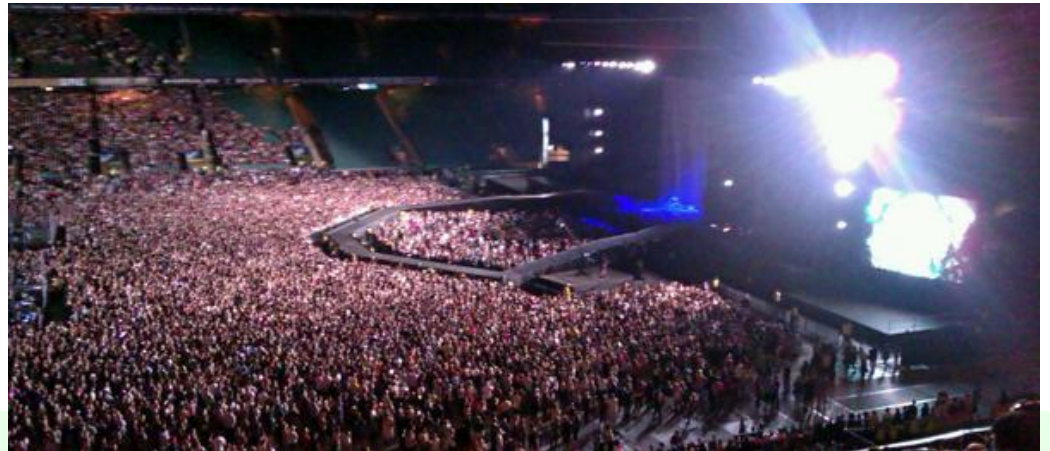
# Flipping correlations

- Discovery of contrasting situations between ancestor and descendant itemsets
  - Identify exceptional or unexpected situations
- Itemsets characterized by a correlation type
  - Positive, negative, or null
  - Correlation strength measured by correlation indices
    - Kulczynsky, lift, ...
- Itemsets whose *correlation type flips* (changes) when its items are generalized to a higher level of abstraction



# Flipping correlations

- Twitter dataset on Music topic
- Flipping correlation
  - Generalized itemset, *negative* correlation  
(Date: Working day), (Location: Twickenham Rugby Stadium)
  - Exception, *positive* correlation  
(Date: 2012-09-08), (Location: 51.45542-0.34165)
  - Lady Gaga sold-out concert in the stadium on 2012-09-08

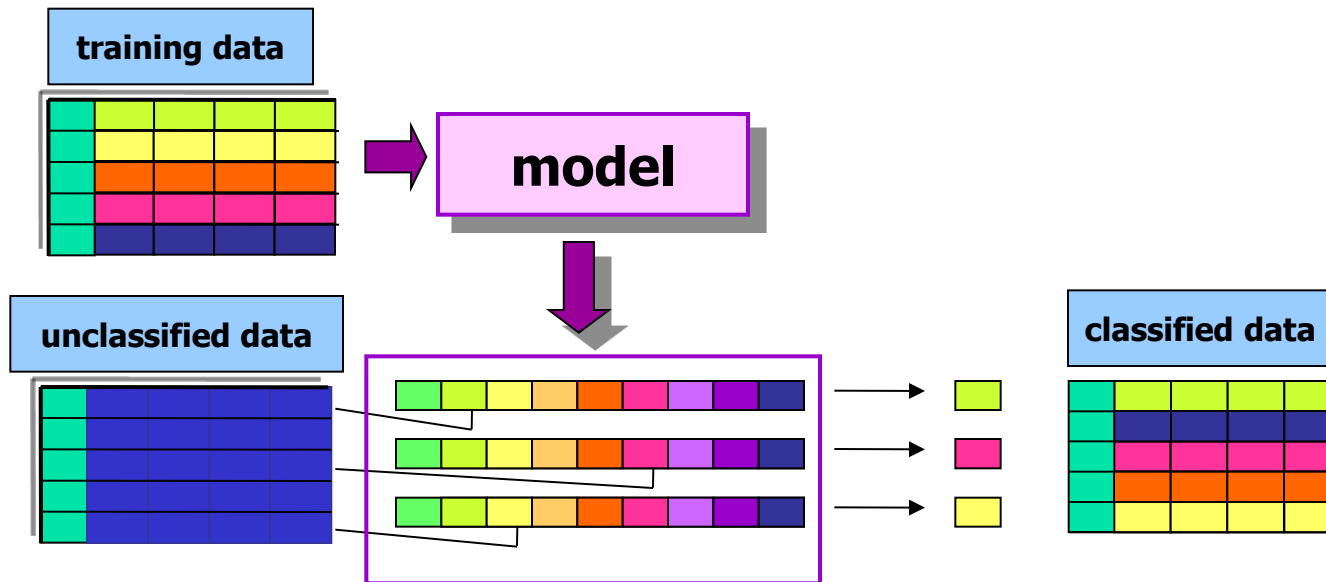




# Classification

## ■ Objectives

- prediction of a (discrete) class label
- definition of a model of a given phenomenon
  - interpretable?





# Rule patterns for classification

- Targets
  - Defining an *interpretable* rule *model* capable of
    - assigning class label to unclassified object
    - describing main class characteristics
  - Providing *reasons for* a *classification* outcome
    - why a class label is assigned to a given instance?
- Several types of rules
  - Class association rules (CARs)
    - Good quality classification models
    - Many different approaches



# Class Association Rules

- Structure of “classical” association rules

$$X \rightarrow Y$$

where Y is a class label

- CARs selection
  - Rule selection & sorting
    - based on support, confidence and lift thresholds
  - Rule pruning
    - Database coverage: the training set is covered by selecting topmost rules according to previous sort



# Lazy pruning

- L<sup>3</sup>: Live and Let Live
  - Low support threshold for rule extraction
    - Rule selection based on confidence
  - Multiple support thresholds for different classes
  - Level-based approach in selecting rules
    - *Good rules*, small subset of high quality rules
    - *Spare rules*, larger set of rules not used during database coverage
    - *Harmful rules*, discarded because only wrongly classifying training data
- High quality model
  - Larger rule set, considering spare rules





# Instance-centric approaches

## ■ DeEPs

- Emerging Pattern are patterns that sharply differentiate one (training) class from the others
  - Interesting patterns occur frequently in one class and less frequently in the others
- *Lazy* classification
  - EP extraction takes place for the given test instance
  - Aggregate supports of extracted EPs assign class label

## ■ Harmony

- Selects a subset of best possible rules for each training instance
  - highest confidence frequent covering rules



# The challenge of big data

- Huge data collections exacerbate the problem
  - Very sparse datasets
    - Support threshold setting
  - Computational challenge
    - Scalability in item cardinality is a challenge
    - Hadoop/Spark framework not straightforwardly usable
- Local exploration of datasets
  - Several criteria to select area to explore
    - Rule constraints
      - Schema constraints, item constraints
    - Predicates on attributes
    - Instance constraints



# Rules as building blocks

- Rules may support black box learning paradigms
  - Learn rule patterns from data
    - learn some abstractions by experience
    - e.g., a positioning rule for objects
  - Use learned patterns (abstractions) to support deep learning techniques
    - drive learning also by abstractions
    - e.g., use rule to improve object detection
- It is the way our brain works!



# Thanks to...

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Questions?

